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Aerospace Environmental Support Center

Technical Memorandum 70-3

IONOSPHERIC ELECTRON DENSITY PROFILE MODEL

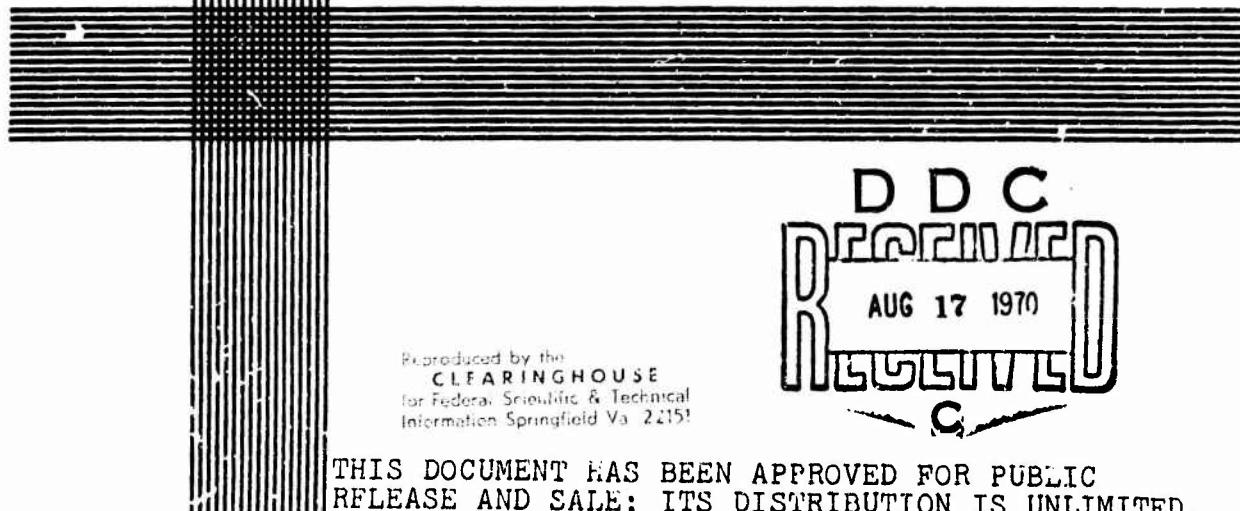
July 1970

by

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1. Preface.

Recent investigation of the effects of ionospheric retardation and refraction on satellite tracking radars has generated a need for a means to predict the errors and correct for them. This paper describes a project undertaken by 4th Weather Wing to produce a realistic electron density profile based upon parameters which can be forecast reasonably accurately. The authors wish to acknowledge the help provided them in this project. Lt Colonel Hansrote provided the impetus for producing such a model. Capt Jack Wrobel solved our initial problems of scale height by providing "Wrobel's Equation." MSGt Birch and TSgtuster analyzed and evaluated the model against actual observations. Mrs. Green accomplished the manuscript typing. Thanks, also to Lt Bo Eross for his system analysis suggestions.

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### II. Introduction.

The development of a computer program for predicting electron density profiles was prompted by the realization that ionospheric retardation and refraction produced errors in range and azimuth of satellite tracking radars. These errors are of the same order of magnitude as those produced by tropospheric effects when the UHF radars are operating above a few degrees elevation. Since the effects are rather small, it was assumed that a simple model from 100 km to 1000 km would be sufficient. However, as development work began, other requirements for electron density profiles became apparent. A three-dimensional ionosphere for HF ray tracing which requires considerably more accuracy in the lower ionosphere, was requested. In addition, total electron content for correcting for Faraday rotation in some navigational satellites requires a model extending higher than 1000 km.

The program described in this report has been used routinely for about eight months to predict electron density profiles for the FPS-85 radar at Eglin AFB, Fla. Results are encouraging enough to warrant publication. It should be considered an interim report, however, as improvements are sure to be required as its accuracy is evaluated for different purposes.

### III. Development.

The ionospheric electron density profile model presented in this paper consists of the sum of three Chapman layers (E, F1, and F2). Each layer is of the form

$$N_h = N_{\max} \exp [a[1-Z-\exp(-Z)]]$$

where  $Z = (h-h_{\max})/h_s$

$N_h$  = electron density at height  $h$

$N_{\max}$  = electron density at the peak of the Chapman layer  $h_{\max}$

$h_s$  = scale height at the peak (except for the topside of the F2 region)

The value of the constant,  $a$ , depends upon whether electrons are lost by attachment or by recombination. While neither process is unique in any layer,  $a$  is assumed to be 0.5 for the E-layer and 1.0 for the F1 and F2 layers.

Electron densities in the topside ionosphere are controlled by complex motions rather than a production-loss balance and cannot be successfully described strictly by a Chapman layer. An effort was made to keep from over-complicating the model and still obtain the best topside profile. After some experimentation a fit was obtained by simply using the Chapman equation for the topside ionosphere, but computing the electron densities by using a variable scale height throughout the region.

The scale height profile is calculated from the equation

$$h_s = \frac{\log h}{2.186 \times 10^{-2}} - 203.447$$

This equation describes the scale height of a simple standard atmosphere and was derived by Capt J. Wrobel (private communication).

Critical frequencies for the E and F1 regions are determined from regression equations [1], [2].

$$f_{\text{o}}E = 0.9[(180 + 1.44R) \cos x]^{0.25}$$

$$f_{\text{o}}F1 = 1.26f_{\text{o}}E + 0.5$$

where  $R$  = the twelve-month running mean sunspot number

$x$  = the solar zenith angle

When  $x$  exceeds  $90^\circ$ ,  $f_{\text{o}}E$  is set to 0.7 MHz. When  $x$  exceeds  $135^\circ$ ,  $f_{\text{o}}E$  is set to 0.3 MHz.

The F2 region critical frequency may be predicted from the ITS (ESSA) coefficients by predicting a sunspot number ( $R$ ) [1]. It may also be predicted manually on a short-term basis by the Air Force Aerospace Environmental Support Center. For post analysis purposes, an observed value may be used.

The height of the peak of the E region is assumed to be 120 km. After some experimentation, the F1 peak was placed halfway between the E and F2 peaks.

The height of the F2 peak is calculated by using Shimazaki's equation [3]:

$$h_{\max} = \frac{1490}{M} - 176$$

where the  $M(3000)$  factor,  $M$ , may be predicted in a manner similar to the prediction of  $f_{\text{o}}F2$ , or observed. Computations of  $h_{\max}$  using  $M(3000)$  were found to be accurate within 20 km at mid latitudes. If a more accurate measure of  $h_{\max}$  is available,

such as  $h_p F2$ , an artificial  $M(3000)$  may be calculated from the Shimazaki equation and used as an input into the computer program.

#### IV. Description of the Computer Program.

A copy of the computer program used to compute an electron density profile is listed in Appendix A. The program is written in IBM 7090 FORTRAN IV. There are three input options (all of which are concerned with the method of obtaining  $foF2$  and  $M(3000)$ ). Two output options are available, depending upon the representation of the profile required.

The program computes electron densities independently for each of three regions ( $E$ ,  $F1$  and  $F2$ ). The base of the profile is 100 km and computations are made at 5 km increments to 1000 km. The three regions are added together to give the total electron density at each increment of altitude. Electron density is not permitted to decrease with altitude, but is held constant across "valleys" in the profile.

Total electron content in a one square meter cross section up to a given altitude is also computed. An initial electron content is established at 95 km, to represent the total content below 100 km. A calculation of plasma frequency is made from the electron density for each 5 km interval.

Input parameters are read from data cards. The first data card indicates output options (Table 1). The second data card contains information pertaining to the geographic location of the profile. The format of the card is the same for all input options (Table 2).

As previously mentioned, there are three input options which determine the method by which  $foF2$  and  $M(3000)$  are introduced into the program. Data card number 3 contains information pertinent to the profile, including the input option variable IOPT. Table 3 lists the input parameters on the third data card and indicates which of them are used by the program under each of the three input options. If  $IOPT = 1$ ,  $foF2$  and  $M(3000)$  are computed from a card deck of ITS Prediction Coefficients. (Subroutines used to compute  $foF2$  and  $M(3000)$  from ITS coefficients were extracted from a program published in [4].) If  $IOPT = 2$ , a long-term data tape containing sunspot dependent coefficients of  $foF2$  and  $M(3000)$  is read to determine  $foF2$  and  $M(3000)$ . Finally, if  $IOPT = 3$ ,  $foF2$  and  $M(3000)$  are read explicitly from the data card.

TABLE 1

<u>Card Column</u>	<u>Variable</u>	<u>Explanation</u>
1	IPILOT	If IPILOT = 1, a profile of plasma frequency vs height is plotted. If IPILOT = 0, plot is suppressed.
2	IPNCH	if IPNCH = 1, the 17 most significant points depicting the profile are punched onto data cards. If IPNCH = 0, the punch routine is suppressed.

TABLE 2

<u>Card Column</u>	<u>Variable</u>	<u>Explanation</u>
1-6	CLAT	Latitude
7	NORS	Hemisphere (N, S)
8-13	CLONG	Longitude
14	IHEM	Hemisphere (E, W)
15-38	NAME	Name of Station

TABLE 3

<u>Card Column</u>	<u>Variable</u>	<u>Required Under Option</u>	<u>Explanation</u>
1-2	IYR	1, 2, 3	Year
3-4	MNTH1	1, 2, 3	Month
5-6	MNTH2	1, 2	Used if mean of two months coefficients are required.
7-8	IDA	3	Day
9-12	IBHR	1, 2, 3	Beginning time of set of consecutive profiles (GMT).
13-16	IEHR	1, 2, 3	Ending time of set of consecutive profiles (GMT).
17-18	INC	1, 2, 3	Increment of time step (hours).
19-21	JDAY	1, 2, 3	Julian Day
22	IOPT	1, 2, 3	Option
26-30	SSN	1, 2, 3	Sunspot Number
31-40	FOF2	3	f <sub>OF2</sub> (explicit) MHz and tenths
41-50	EM3000	3	M(300) explicit hundredths
51-56	IVB	1, 2	Beginning of valid time (i.e., 10 May).
57-62	IVE	1, 2	Ending of valid time (i.e., 20 May).

NOTE: All numbers are integers except SSN, FOF2, and EM3000. These three are floating point, punched with a decimal point, anywhere in the field.

## V. Description of the Computer Produced Profile.

Appendix 2 is a sample profile produced by computer. The profile is in four sections. The first section provides a summary of input data and pertinent information for each of the three regions. The second section is the profile itself, listing values of height, E-region density, F1-region density, F2-region density, total density, cumulative electron content, plasma frequency and scale height for each 5 km increment of the model. Output of the third section depends upon the value of the output option IPLOT (see Table 1), and plots a graph of plasma frequency vs height for the model. The fourth and final section depends upon the value of the output option IPNCH. If selected, the 17 most significant values of plasma frequency describing the profile are chosen objectively and written onto magnetic tape for punching onto data cards. In addition, a checklist of the points selected is printed.

## VI. Evaluation of the Model.

An evaluation of this model was made by comparing with observed electron density profiles and with total electron content measurements.

Figures 1 to 8 show model monthly median profiles for Wallops Island, Va., during 1968, compared with the observed profiles available from World Data Center A, Boulder, Colorado. Excellent results are obtained during winter and at night. The July 1800Z (mid-day) is the worst case among several dozen such comparisons at various locations and times.

In Table 4, the total electron content calculated to 1000 km is compared with observations of total content from Bedford, Mass., to geostationary satellites, a path which passes through the F2 peak near Wallops Island. These observations, courtesy of Jack Klobuchar, Air Force Cambridge Research Laboratories, are converted to vertical incidence by assuming a cosine correction factor. As expected, the model is generally lower than the observations since it cuts off at 1000 km. It is interesting to note that in the summer daytime, when the model overestimates the bottomside content (Figure 6), it underestimates the total content. This implies that more electrons are present in the topside than the model predicts.

A third comparison is shown in Figure 9. Here, total content to 1000 km from the model is compared with the total content on near vertical incidence paths to synchronous satellites in the vicinity of Hawaii [5]. The shape of the diurnal curve is good and the results are again excellent at night but are underestimated at midday.

TABLE 4  
TOTAL ELECTRON CONTENT  
( $10^{-3}$  M $^{-2}$ )  
WALLOPS ISLAND 1968

<u>GMT</u>	<u>OBSERVED TEC</u>	<u>MODEL TO 1000 KM</u>	<u>PERCENT DIFFERENCE</u>
<b>January</b>			
0100	1.2	1.0	-10
0500	.66	.56	-15
2000	4.1	3.5	-15
<b>March</b>			
0200	1.6	1.4	-13
0500	.98	.95	-3
1100	.65	.61	-6
1600	3.3	3.2	-3
2100	3.7	3.4	-8
<b>May</b>			
0300	1.5	1.4	-7
0700	.85	.93	+9
1200	1.4	1.2	-14
1600	2.3	2.0	-13
2200	2.7	2.1	-22
<b>July</b>			
0400	1.2	1.1	-8
0800	.62	.60	-3
1300	1.4	1.3	-7
1800	1.8	1.6	-11
2300	2.1	1.6	-24
<b>September</b>			
0100	1.4	1.4	0
0500	.91	.89	-2
1000	.42	.46	+10
1500	2.4	2.4	0
2000	2.9	2.7	-7
<b>November</b>			
0200	.75	.65	-13
0600	.55	.52	-5
1100	.39	.36	-8
1600	3.2	3.3	+3
2100	3.2	2.8	-13

## VII. Summary and Conclusion.

The electron density profile model came about as an attempt to produce a reasonably simple method of predicting electron densities in the 100-1000 km range. This model should not be considered final, by any means, even for the current applications. The scale height profile should be improved to include diurnal and seasonal variations. The model should be extended from its upper limit of 1000 km to the plasmapause. Variations of electron density with geomagnetic activity should be included. Improved prediction or specification of any of the input parameters will, of course, improve the accuracy of the profile model. The height of the F2 maximum is probably the most important of these.

VIII. References.

1. Barghausen, A. F., J. W. Finne", L. L. Proctor, and L. D. Shultz (1969), Predicting Long-Term Operational Parameters of High-Frequency Sky-Wave Telecommunications Systems, ESSA Technical Report ERL 110-ITS 78.
2. Haydon, G. W. and D. L. Lucas (1968), "Predicting Ionospheric Electron Density Profiles," Radio Science, Vol 3 (New Series) No 1, III.
3. Shimazaki, T. (1955), "World-Wide Daily Variations in the Height of the Maximum Electron Density of the Ionospheric F2 Layer," J. Radio Res. Labs, Japan, 2, 85-97.
4. Jones, W. B., R. P. Graham, and M. Leftin (1969), Advances in Ionospheric Mapping by Numerical Methods, ESSA Technical Report ERL 107-ITS 75.
5. Yuen, P. C. and T. H. Roelofs, Atlas of Total Electron Content Plots, Vol 3, Radio Science Lab, University of Hawaii, Honolulu.

UNCLASSIFIED

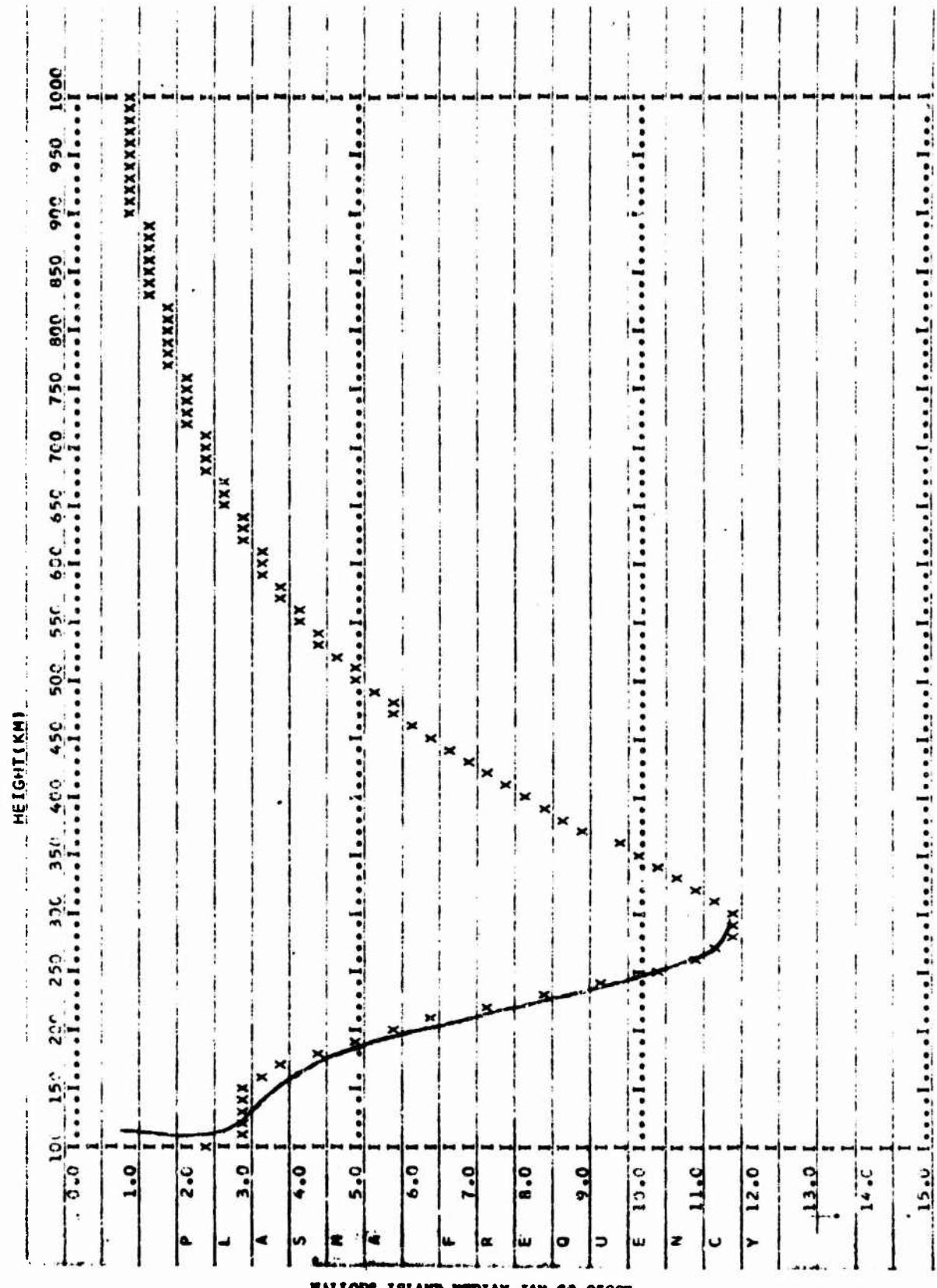
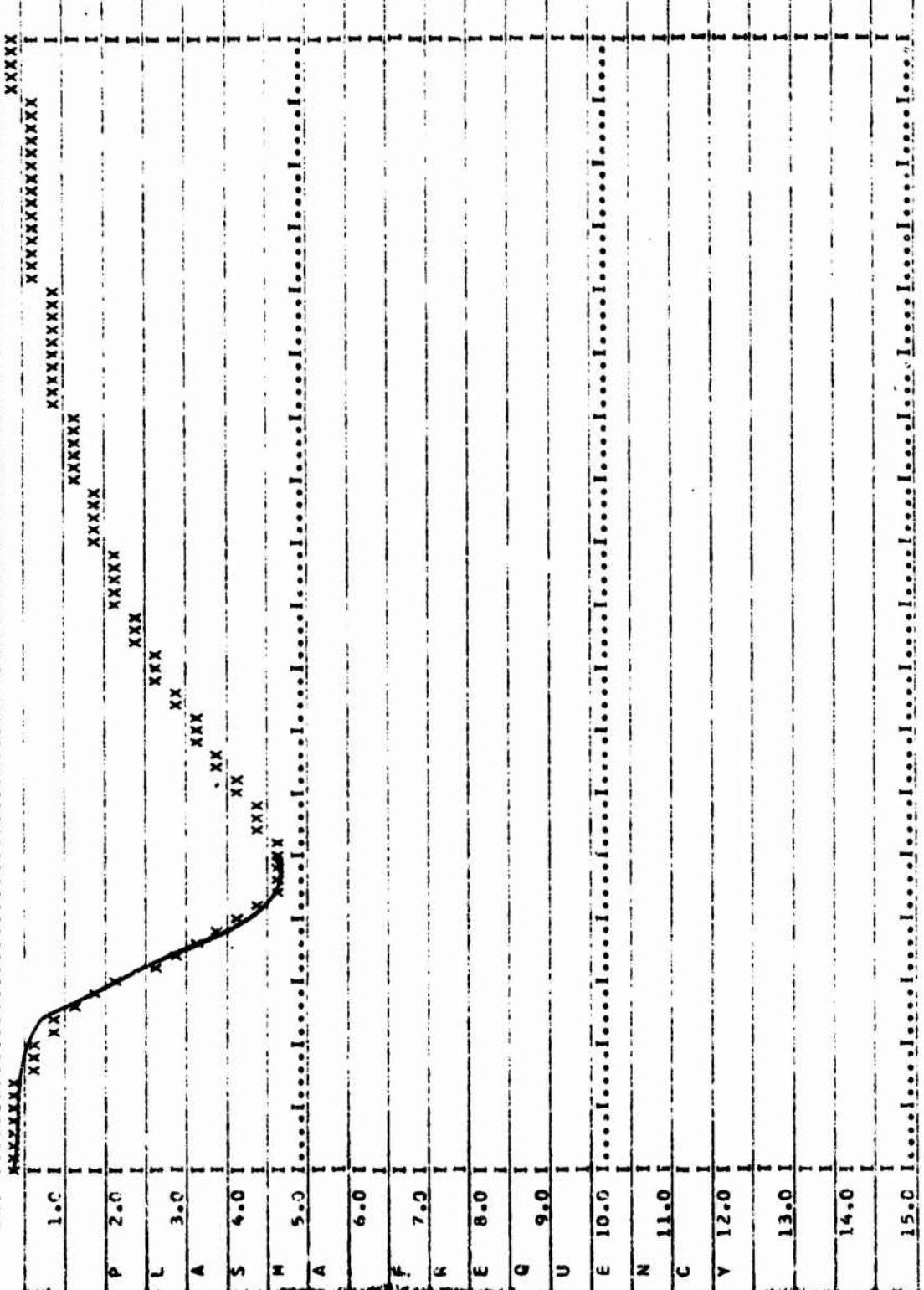


Figure 1

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HEIGHT (KM)

100 150 200 250 300 350 400 450 500 550 600 650 700 750 800 850 900 950 1000



WACOM DRAWING SOFTWARE 6.0 20002

Figure 2

UNCLASSIFIED

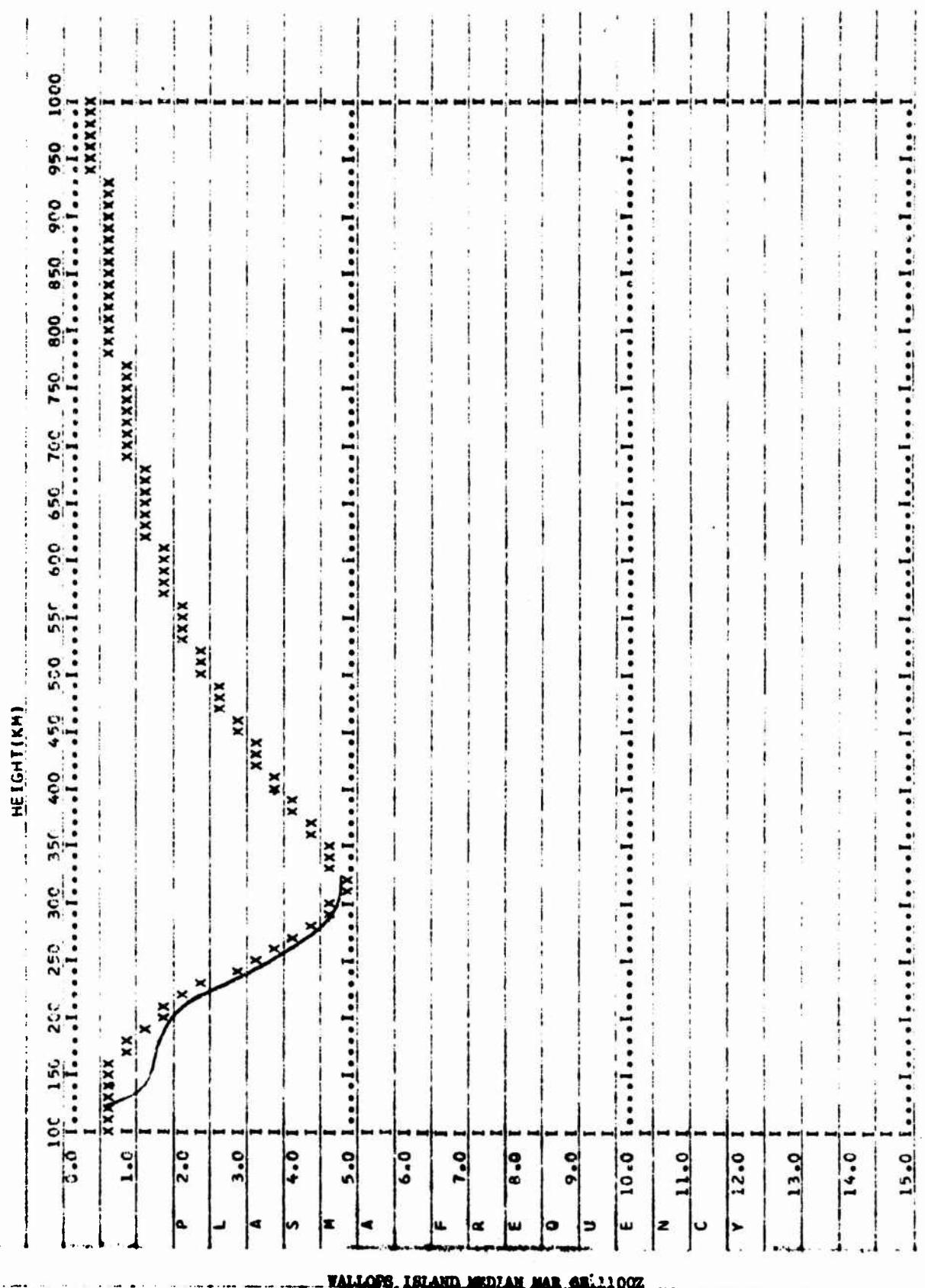
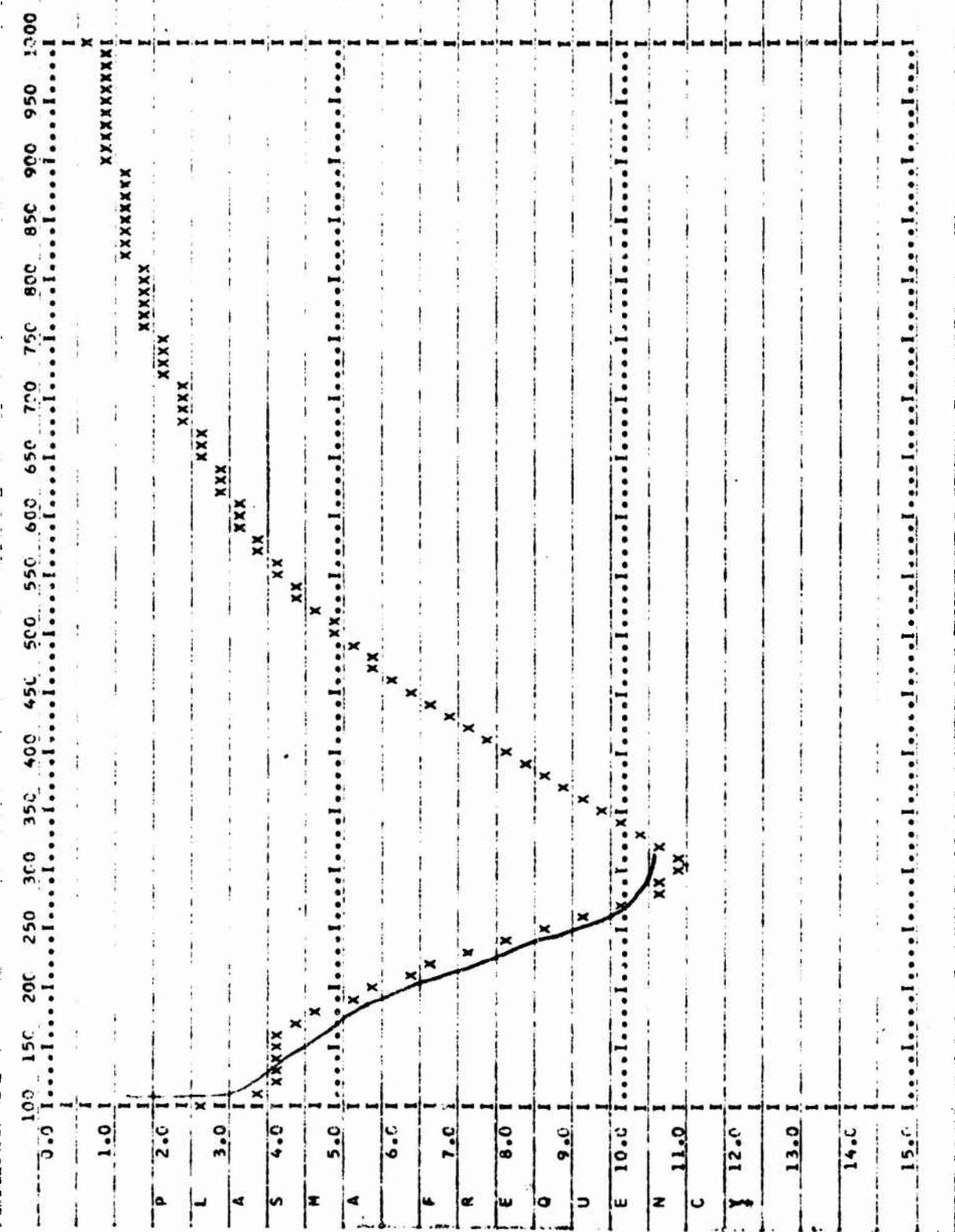


FIGURE 3

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HEIGHT (MM)

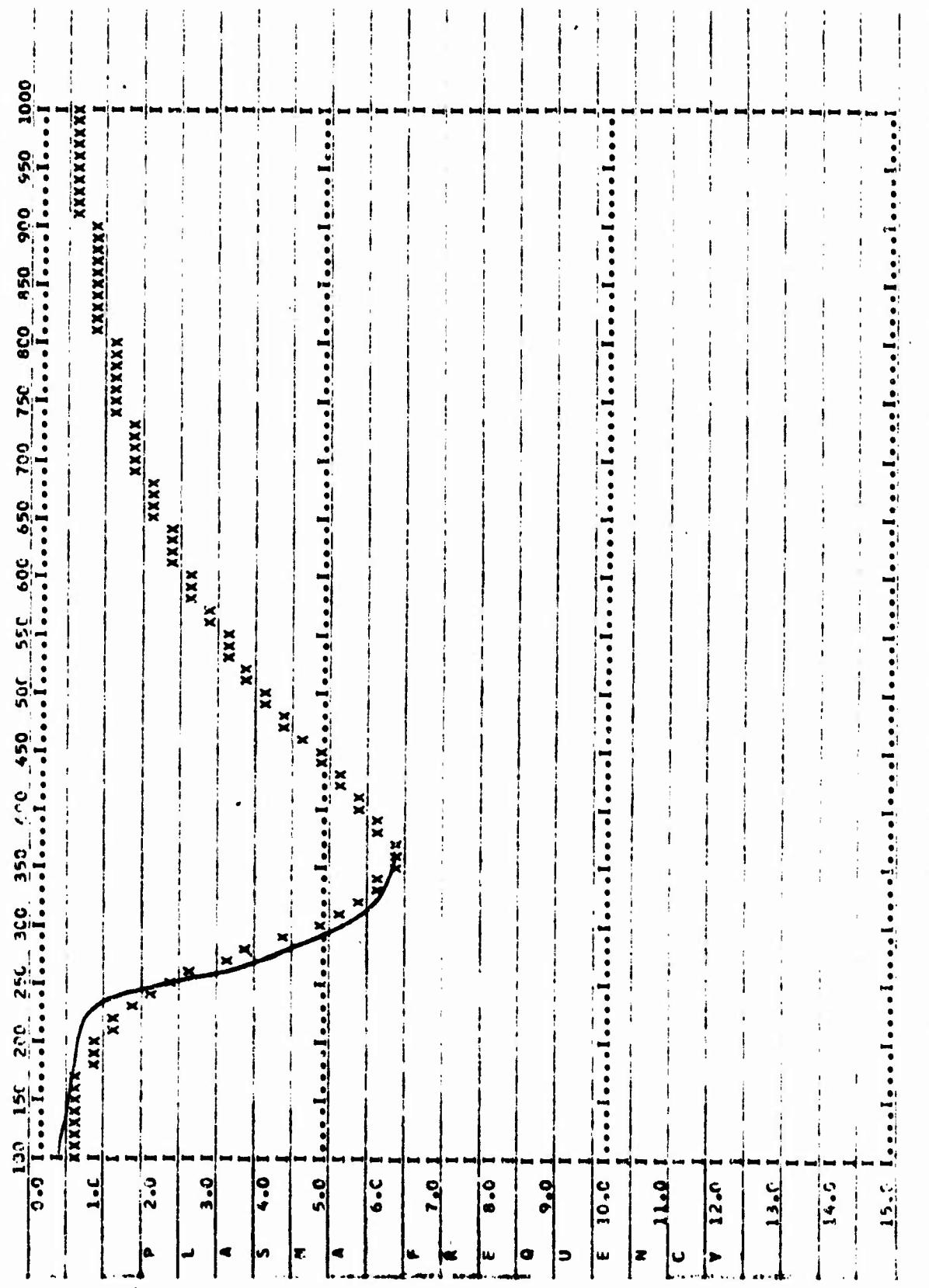


WALLOPS ISLAND MEDIAN MAP 68 1600Z

Figure 4

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WEIGHT(MM)



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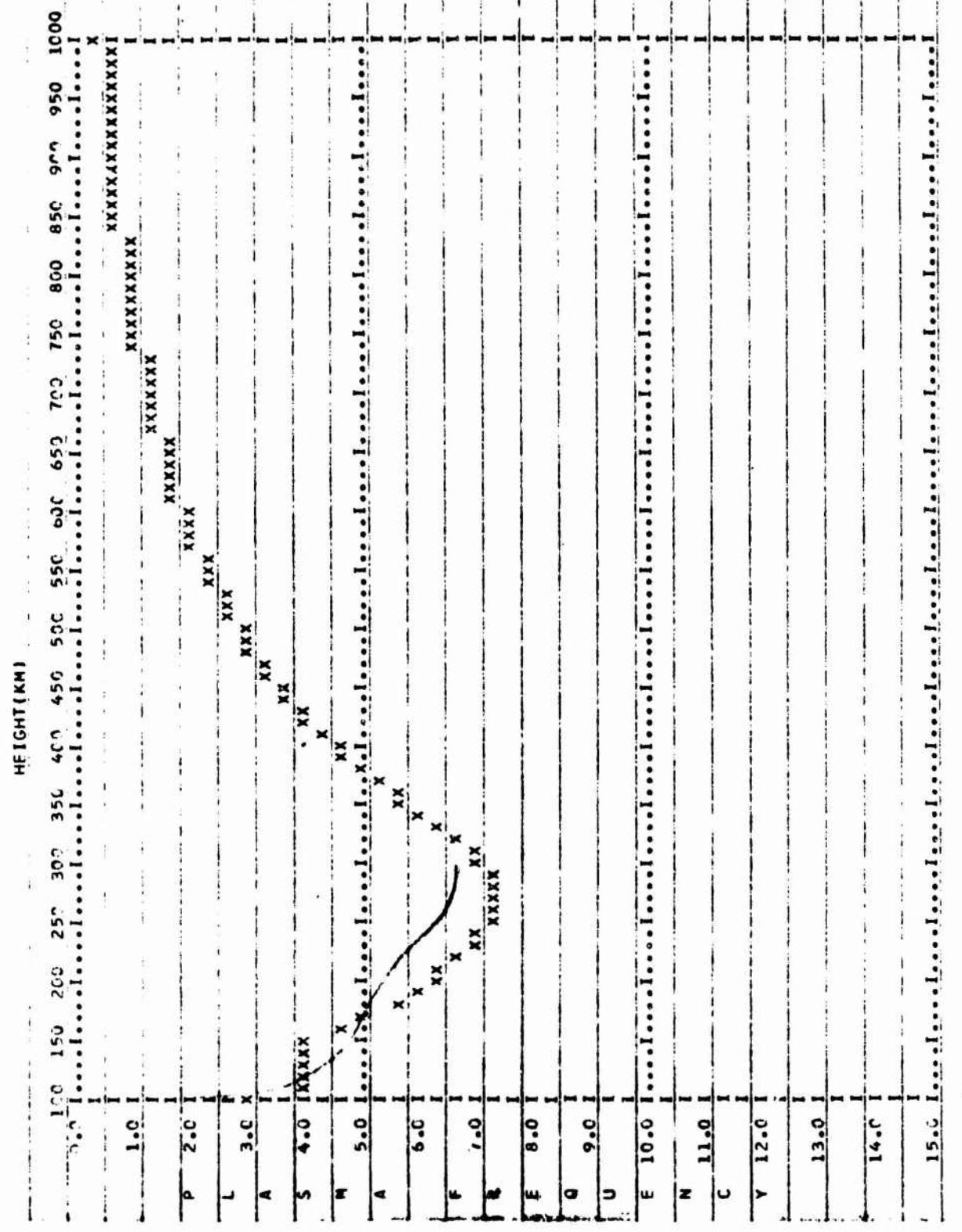


Figure 6

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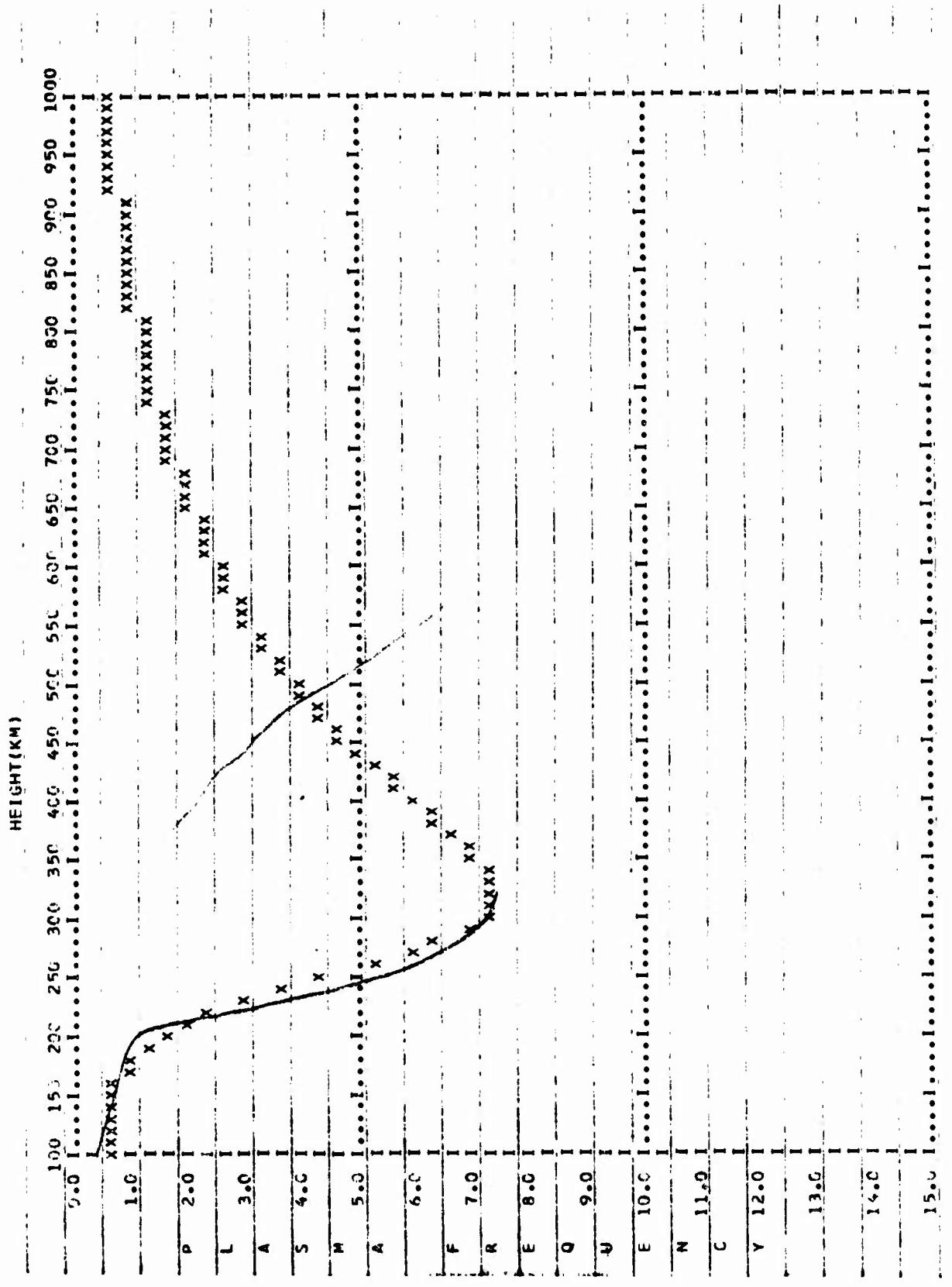
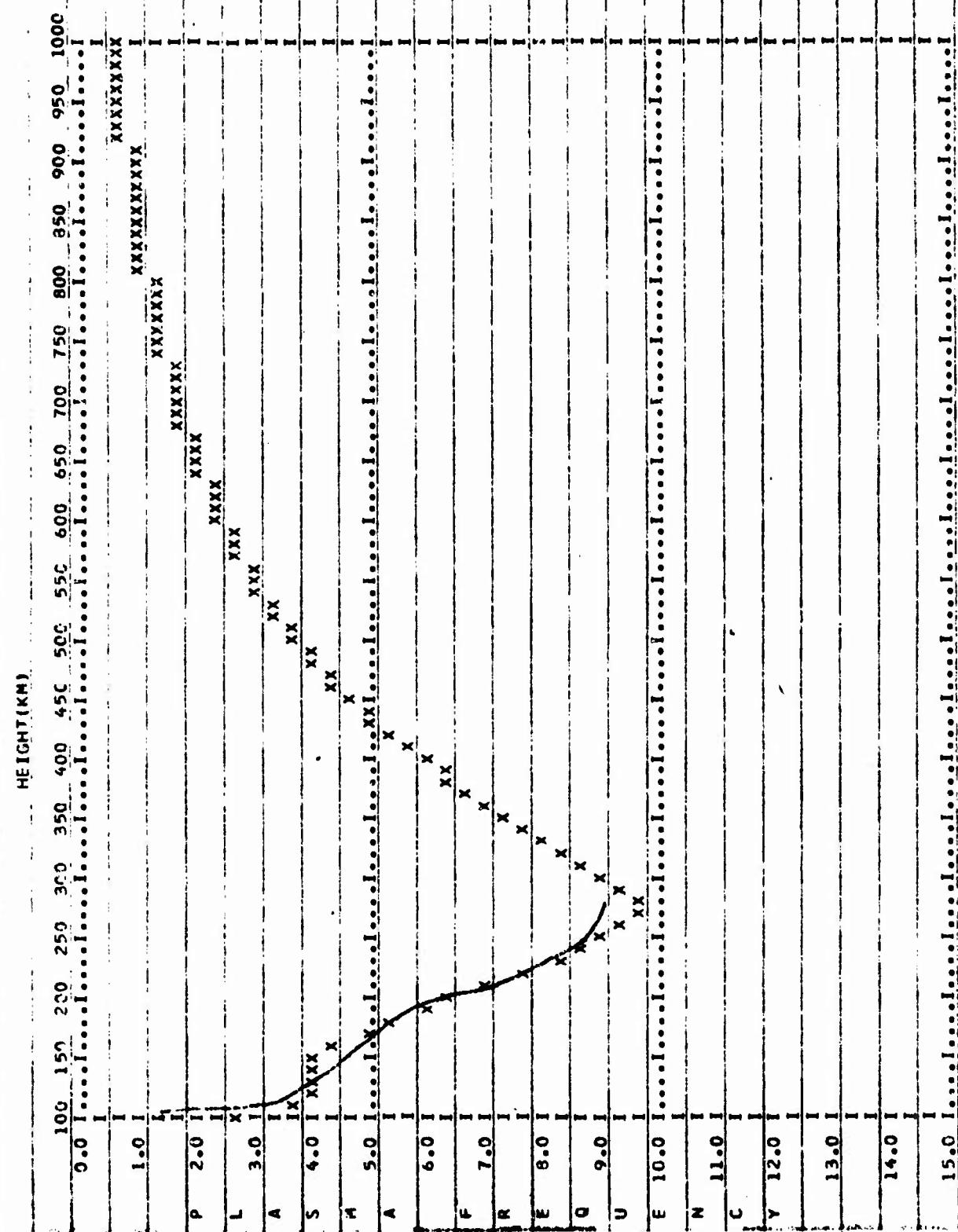


Figure 7

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FALLORS ISLAND MEDIAN SEP 68 1500Z

Figure 8

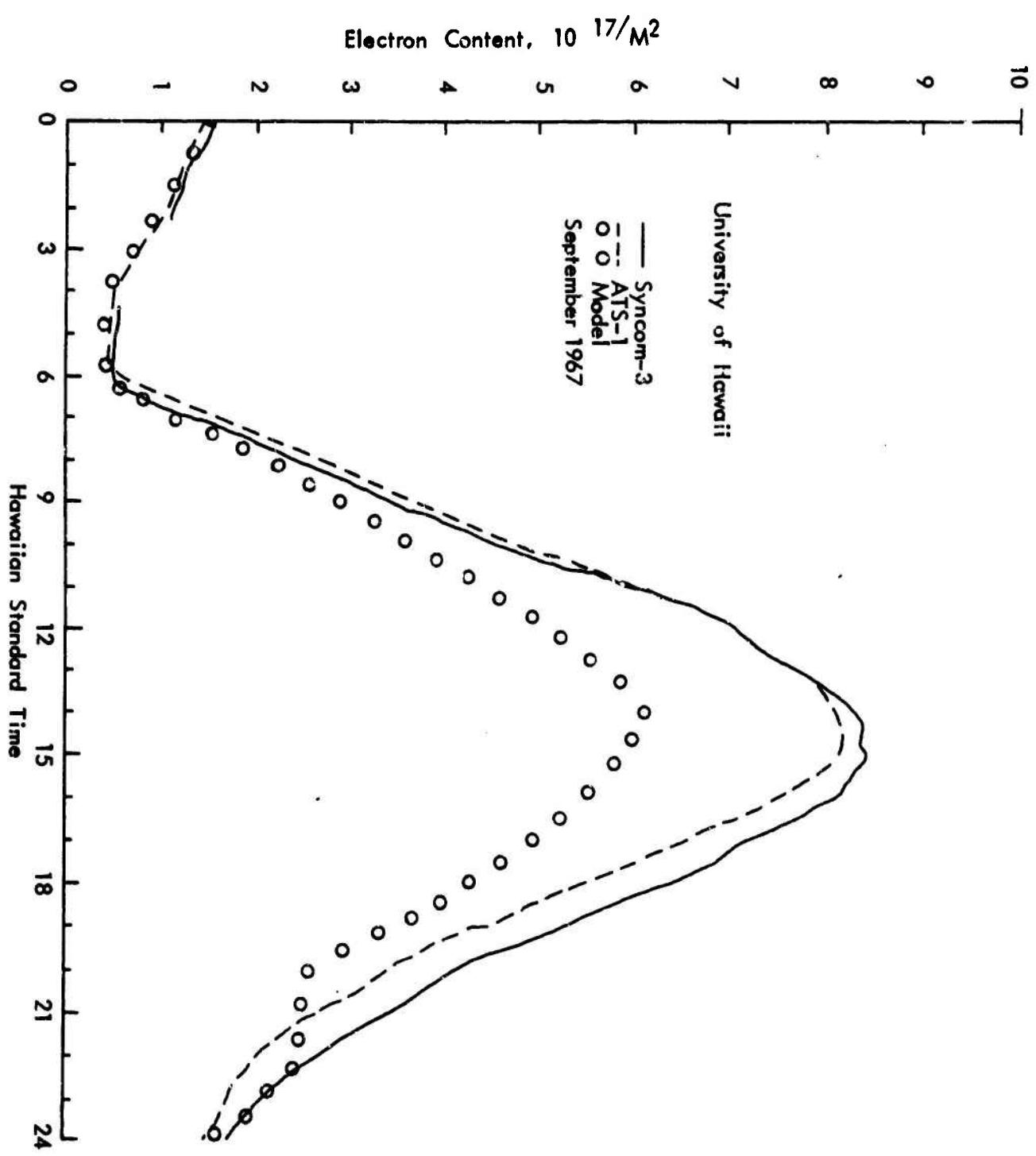


FIGURE 9

## **Appendix A**

**Computer Program  
"MODEL"**

```

SIBFIG MODEL
DIMENSION SCALE(182),IHGT(182)
DIMENSION VAL(91),NAME(4),STOR(182)
COMMON /H/ K(14),U(17,76),KX(14),UX(17,76),KI(14),KXI(14),
IUI(17,76),UXI(17,76)
DATA IE,IS/1HE,1HS/
C
C***** SET UP CONSTANTS FOR RADIAN CONVERSION *****
C
C180=3.1415927
PI2=C180/2.0
AK=C180/180.0
BK=180.0/C180
GLT=1.36135662
GLG=1.22173030
KARL=0
C
C***** SCALE HEIGHT COMPUTATION (WROBEL-S EQUATION) *****
C
H=95.
DO 10 I=1,182
SCALE(I)=( ALOG(H)/2.186E-02)-203.447
IHGT(I)=H
IF(I.EQ.1) SCALE(I)=6.6
10 H=H+5.0
C
C*****READ OUTPUT OPTIONS *****
C
READ (5,11) IPLOT,IPNCH
11 FORMAT (2I1)
C
C*****READ LOCATION OF STATION *****
C
999 READ (5,4) CLAT,NORS,CLONG,IHEM,(NAME(I),I=1,4)
4 FORMAT (2(F6.1,A1),4A6)
C
C***** CHECK FOR BLANK CARD (END OF ALL DATA) *****
C
IF(CLAT.EQ.0.0) GO TO 777
C
C***** CHECK FOR EASTERN OR SOUTHERN HEMISPHERE *****
C
IF(NORS.EQ.1) CLAT=-1.*CLAT
IF(IHEM.EQ.1) CLONG=-1.0*CLONG
8000 READ (5,44) IYR,MNTH1,MNTH2,IDA,IBHR,IEHR,INC,JDAY,IOPT,SSN,FCF2,
ITEM3000,IVB,IVE
44 FORMAT (4I2,2I4,I2,I3,I1,3X,F5.1,2F10.5,2A6)
IHR=IBHR
INC=INC*100
C
C***** CHECK OPTION 1 = ITS COEFFICIENTS READ FROM CARDS
C          2 = LONG TERM DATA TAPE
C          3 = FCF2 AND M(3000) EXPLICIT *****
C

```

```

IF(IOPT.EQ.1.AND.KARD.EQ.0) GO TO 1
IF(IOPT.EQ.1.AND.KAKD.EQ.1) GO TO 34
IF(ICPT.EQ.2) GO TO 2
IF(IOPT.EQ.3) GO TO 3
GO TO 33
C
***** IOPT = 1, READ CARDS *****
C
1 CALL READU(K,U)
CALL READU(KX,UX)
IF(MNTH2.GT.0) CALL READU(K1,U1)
IF(MNTH2.GT.0) CALL READU(KX1,UX1)
KARU=1
GO TO 34
C
***** IOPT = 2, READ LONG-TERM DATA TAPE *****
C
2 CALL LTAPE(MNTH1,SSN,K,U,KX,UX)
IF(MNTH2.GT.0) CALL LTAPE(MNTH2,SSP,K1,U1,KX1,UX1)
34 CONTINUE
800 CALL DOIT(SLAT,CLONG,IHR,FOF2,EM3000,MNTH1,MNTH2)
GO TO 3
33 WRITE(6,333)
333 FORMAT(1H1,13HERROR IN IOPT)
GO TO 777
J CONTINUE
C
***** IOPT = 3, BEGIN COMPUTATIONS *****
C
C
***** NOW HAVE FOF2 AND M3000 BY ONE OF THREE METHODS *****
C
C
***** CALCULATE SOLAR ZENITH ANGLE *****
C
IFRST=IHR/100
SECND=IHR-IFRST*100
SECND=SECND/60.
GMT=FLCAT(IFRST)+SECND
IF(GMT.EQ.0.0) GMT=24.
L=JDAY
SSP=-23.45*COS((D+10.)/365.*C180*2.)
SSP=SSP*AK
SSL=15.0*GMT-180.0
Z=(SSL-CLONG)*AK
COMP=SIN(CLAT*AK)*SIN(SSP)+COS(CLAT*AK)*COS(SSP)*COS(Z)
COMP=ACOS(COMP)
COMP=ABS(COMP)
RANG=COMP
ZANG=COMP*BK+0.5
C
C
***** CALCULATE GEOMAGNETIC LATITUDE *****
C

```

```

GAT=ARCCOS(SIN(GLT)*SIN(CLAT*AK)+COS(GLT)*COS(CLAT*AK))
I=CCS(CLONG*AK-GLG)
GLAT=(PI2-GAT)*BK
R= SSN

C***** NOW HAVE NEEDED PARAMETERS FOR EQUATIONS *****
C
C
C***** HEIGHT OF E-REGION SET TO 120 KM *****
C
HE=120.0
C
C***** COMPUTE SCALE HEIGHT OF E-REGION *****
C
TE=(ALOG(HE)/2.186E-02)-203.447
C
C***** COMPUTE FOE *****
C
PART=0.9*((180.0+L44*R)*COS(RANG))
IF(PART.GE.0.) FOE=PART+0.25
IF(PART.LT.0.) FOE=0.7
C
C***** IF SOLAR ZENITH ANGLE GREATER THAN 130 DEG, FOE SET TO 0.3 *****
C
IF(ZANG.GE.90.0) FOE=0.7
C
C***** IF SOLAR ZENITH ANGLE GREATER THAN 90 DEG, FOE SET TO 0.7 *****
C
IF(ZANG.GE.130.) FOE=0.3
C
C***** COMPUTE FOF1 *****
C
FOF1=1.26*FOE+0.5
C
C***** COMPUTE MAX DENSITY OF E-REGION *****
C
ENE=1.24E04*(FOE)**2
C
C***** COMPUTE MAX DENSITY OF F1-REGION *****
C
FNMAX=1.24E04*(FOF1)**2
C
C***** COMPUTE MAX DENSITY OF F2-REGION *****
C
ENMAX=1.24E04*(FOF2)**2
C
C***** COMPUTE HEIGHT OF MAX DENSITY (SHIMAZAKI EQUATION) *****
C
HMAX=1490.0/EM3000-176.0
C
C***** COMPUTE SCALE HEIGHT OF F2-REGION *****
C
TF=(ALOG(HMAX)/2.186E-02)-203.447

```

```

C
***** HEIGHT OF F1-REGION SET TO MIDPOINT OF E- AND F2-REGIONS *****
C
HMAX1=(HMAX+120.)/2.

C
***** COMPUTE SCALE HEIGHT OF F1-REGION *****
C
TF1=(ALOG(HMAX1)/2.186E-02)-203.447
IF(IOPT.LT.3) WRITE(6,990) IVB,IVE,IYR,IHR
IF(IOPT.EQ.3) WRITE(7,991) IYR,MNTH,IQA,IHR

C
***** OUTPUT SECTION *****
C
C
***** WRITE HEADING FOR SUMMARY PAGE *****
C
990 FORMAT(1H1,26HIONOSPHERIC PROFILE VALID ,A6,2X,A6,2X,I2,I5,1H2)
99 FORMAT(1H1,24HIONOSPHERIC PROFILE FOR ,3I3,I5,1H2)
      WRITE(6,100) CLAT,NORS,CLONG,IHEM,(NAME(I),I=1,4)
100 FORMAT(1H0,17HSTATION LOCATION ,2F6.1,A1)//15X,4A6)
      IF(IOPT.EQ.1) WRITE(6,1000)
      IF(IOPT.EQ.2) WRITE(6,1001)
1001 FORMAT(1H0,43HTHIS PROFILE BASED UPON LONG-TERM DATA TAPE)
1000 FORMAT(1H0,7X, 40HTHIS PROFILE BASED UPON ITS COEFFICIENTS)
      WRITE(6,101) FOF2,EM3000,FOE,FOF1
101  FORMAT(1H0,7HF0F2 = ,F5.2,10X,8HM3000 = ,F5.2,10X,6HF0E = ,F7.2,
      110X,7HFOF1 = ,F7.2)
      WRITE(6,102) GLAT,ZANG,R
102  FORMAT(1H0,23HGEOGRAPHIC LATITUDE = ,F7.2,5X,
      121HSOLAR ZENITH ANGLE = ,F7.2//1X,17HSUNSPOT NUMBER = ,F5.0)
      WRITE(6,103) TE,HE,ENE
103  FORMAT(1H0,19HVALUES FOR E-REGION//,
      15X,15HSCALE HEIGHT =,F7.2,3H KM/
      25X,9HHEIGHT = ,F7.2,3H KM/
      35X,10HDENSITY = ,F8.0,13H ELECTRONS/CC)
      WRITE(6,1040) TF1,HMAX1,FNMAX
1040 FORMAT(1H0,20HVALUES FOR F1-REGION// .
      15X,15HSCALE HEIGHT =,F7.2,3H KM/
      25X,9HHEIGHT = ,F7.2,3H KM/
      35X,10HDENSITY = ,F8.0,13H ELECTRONS/CC)
      WRITE(6,104) TF,HMAX,ENMAX
104  FORMAT(1H0,20HVALUES FOR F2-REGION//,
      15X,15HSCALE HEIGHT =,F7.2,3H KM/
      25X,9HHEIGHT = ,F7.2,3H KM/
      35X,10HDENSITY = ,F8.0,13H ELECTRONS/CC)
***** WRITE HEADING FOR PROFILE PAGE *****
      WRITE(6,201)

201  FORMAT(1H1,10X,24HELECTRON DENSITY PROFILE//5X,2HKM,5X,
      18HF-REGION,5X,9HF1-REGION,5X,9HF2-REGION,7X,5HTOTAL,7X,
      210HCUMULATIVE,5X,16HPLASMA FREQUENCY,5X,5HSCALE)
      ENP1=0.
      ENSAV=0.

```

```

C ***** COMPUTE AND PRINT VALUES FOR EACH 5 KM LEVEL *****
C
H=95.
DO 200 I=1,182
J=I/2
FZE=(H-HMAX1)/TF1
EZE=(H-HE)/TE
C
C***** ELECTRON DENSITIES COMPUTED FOR F2-REGION BASED ON A
C***** CONSTANT SCALE HEIGHT IF BELOW THE F2-PEAK AND
C***** ON A VARIABLE SCALE HEIGHT IF ABOVE THE F2-PEAK *****
C
IF(H.GT.HMAX) ZEE=(H-HMAX)/SCALE(I)
IF(H.LE.HMAX) ZEE=(H-HMAX)/TF
EE=ENE * EXP(0.5*(1.0-EZE-EXP(-1.0*EZE)))
EN=ENMAX*EXP (1.0-ZEE-EXP(-1.0*ZEE))
FN=FNMAX*EXP (1.0-FZE-EXP(-1.0*FZE))
ENP=EN+EE+FN
IF(H.GT.HE.AND.H.LT.HMAX1.AND.ENP.LT.ENE) ENP=ENE
IF(H.GT.HMAX1.AND.H.LT.HMAX.AND.ENP.LT.FNMAX) ENP=FNMAX
IF(ENP.LT.ENP1.AND.H.LT.HMAX) ENP=ENP1
ENP1=ENP
PLAS=8.97E-03*SQR(T(ENP))
STOR(I)=PLAS
IF(MOD(I,2).EQ.0) VAL(J)=PLAS
ENSAV=ENSAV+ENP*5.0E-9
IF(I.EQ.1) GO TO 200
IH=H
WRITE (6,202) IH,EE,FN,EN,ENP,ENSAV,PLAS,SCALE(I)
202 FORMAT (3X,I4,1X,4(4X,F9.0),5X,1PE16.8,6X,0PF7.2,7X,F7.2)
200 H=H+5.0
C
C***** CALL PLOT ROUTINE IF REQUESTED *****
C
IF(IPLOT.GT.0) CALL PLOT(VAL)
C
C***** CALL PUNCH ROUTINE IF REQUESTED *****
C
IF(IPNCH.GT.0) CALL SIGT(STOR,IHGT,IVB,IVE,IYR,IHR)
C
C***** IF IOPT EQUALS 3, ONLY ONE STATION ANALYZED PER FOF2 AND M(3000
C
IF(IOPT.EQ.3) GO TO 999
C
C***** INCREMENT HOUR *****
C
IHR=IHR+INC
IF(IHR.GT.IEHR) GO TO 999
"n TC 800
C
C***** EXIT AND TERMINATE RUN *****
C
777 CONTINUE
ENDFILE 9
REWIND 9
STOP
END

```



```

$IBFTC SIGNIF
SUBROUTINE SIG(STOR,IHGT,IVB,IVE,IYR,IHR)
DIMENSION STOR(182),IHGT(182),PLASQ(17)
INTEGER HEIT(17)
HEIT(1)=IHGT(2)
HEIT(2)=IHGT(6)
HEIT(15)=IHGT(182)
HEIT(16)=IHGT(22)
PLASQ(16)=STOR(22)
HEIT(17)=IHGT(32)
PLASQ(1)=STOR(2)
PLASQ(17)=STOR(32)
PLASQ(2)=STOR(6)
PLASQ(15)=STOR(182)
DO 1 I=1,181
    IF(STOR(I).EQ.STOR(I+1)) GO TO 4
1   CONTINUE
    HEIT(3)=IHGT(12)
    PLASQ(3)=STOR(12)
    K=12
    GO TO 5
4   HEIT(3)=IHGT(1)
    PLASQ(3)=STOR(1)
    K=I
5   DO 6 I=K,181
    IF(STOR(I+1).NE.STOR(K)) GO TO 7
6   CONTINUE
    HEIT(4)=IHGT(22)
    PLASQ(4)=STOR(22)
    K=22
    GO TO 8
7   HEIT(4)=IHGT(1)
    PLASQ(4)=STOR(1)
    K=I
8   DO 9 I=K,181
    IF(STOR(I).LT.STOR(I+1)) GO TO 9
    HEIT(7)=IHGT(1)
    PLASQ(7)=STOR(1)
    GO TO 10
9   CONTINUE
10  K=I-5
    L=I-10
    LL=I+5
    HEIT(8)=IHGT(LL)
    HEIT(6)=IHGT(K)
    HEIT(5)=IHGT(L)
    PLASQ(8)=STOR(LL)
    PLASQ(6)=STOR(K)
    PLASQ(5)=STOR(L)
    HEIT(9)=IHGT(52)

```

```

      PLASQ(9)=STOR(52)
      K=62
      IF(HEIT(9).GE.370) K=72
      HEIT(10)=IHGT(K)
      PLASQ(10)=STOR(K)
      HEIT(11)=IHGT(82)
      PLASQ(11)=STOR(82)
      HEIT(12)=IHGT(102)
      PLASQ(12)=STOR(102)
      HEIT(13)=IHGT(132)
      PLASQ(13)=STOR(132)
      HEIT(14)=IHGT(162)
      PLASQ(14)=STOR(162)
15     DO 100 I=2,17
      IF(HEIT(I).GE.HEIT(I-1)) GO TO 100
101    ITEMP=HEIT(I)
      HEIT(I)=HEIT(I-1)
      HEIT(I-1)=ITEMP
      TEMP=PLASQ(I)
      PLASQ(I)=PLASQ(I-1)
      PLASQ(I-1)=TEMP
      GO TO 15
190    CONTINUE
      IHR1=IHR-70
      IF(IHR1.LT.0) IHR1=2330
      IHR2=IHR+30
      IHR1=IHR1+10000
      WRITE (9,99) IVB,IYR,IVE,IYR,IHR1,IHR2
      WRITE (6,98) IVB,IYR,IVE,IYR,IHR1,IHR2
99     FORMAT (6HVALID ,A6,I3,3H - ,A6,I3,1X,14,5HZ TO ,14,
      132HZ REMOVE THIS CARD BEFORE USING)
98     FORMAT (1H1,26HIONOSPHERIC PROFILE VALID ,A6,I3,3H - ,A6,I3,1X,I4,
      15HZ TO ,14,1HZ)
      DO 200 I=1,17
      WRITE (5,97) HEIT(I),PLASQ(I)
      WRITE (9,96) HEIT(I),PLASQ(I)
200    CONTINUE
97     FORMAT (1X,4HICNC,12X,I4,F12.2)
96     FORMAT (4HIONO,12X,I4,F12.2)
      RETURN
      END

```

## **Appendix B**

### **Sample Computer Output**

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IONOSPHERIC PROFILE VALID 23 MAY 07 JUN 70 1900Z

STATION LOCATION 24.0N 86.0W

EGLIN RANGE

THIS PROFILE BASED UPON ITS COEFFICIENTS

FOF2 = 9.25 M3000 = 2.76 FOF = 4.04 FOF1 = 5.59

GEO MAGNETIC LATITUDE = 35.48 SOLAR ZENITH ANGLE = 18.11

SUNSPOT NUMBER = 90.

VALUES FOR E-REGION

SCALE HEIGHT = 15.56 KM

HEIGHT = 120.00 KM

DENSITY = 202076. ELECTRONS/CC

VALUES FOR F1-REGION

SCALE HEIGHT = 47.56 KM

HEIGHT = 241.54 KM

DENSITY = 386989. ELECTRONS/CC

VALUES FOR F2-REGION

SCALE HEIGHT = 66.21 KM

HEIGHT = 363.07 KM

DENSITY = 106182. ELECTRONS/CC

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## ELECTRON DENSITY PROFILE

KM	E-WEIGHT	F1-PEGLIN	F2-PEGLIN	IGTAL	CUMULATIVE	PLASMA FREQUENCY	SCALE
100	10.1692	0.	0.	103692.	4.26902699E 14	2.86	7.22
105	1.45409	0.	0.	145610.	1.51195080E 15	3.42	9.45
110	1.7154	2.	0.	17543.	2.44166675E 15	3.74	11.58
115	1.96336	9.	0.	196365.	3.42319402E 15	3.97	13.61
120	2.0216	35.	0.	202111.	4.43304976E 15	4.03	15.56
125	1.97431	113.	0.	202111.	5.4440343E 15	4.03	17.43
130	1.6572	323.	0.	202111.	6.45505816E 15	4.03	19.27
135	1.70021	823.	0.	202111.	7.46561289E 15	4.03	20.95
140	1.52581	1891.	0.	202111.	8.47616756E 15	4.03	22.61
145	1.34966	3959.	0.	202111.	9.48672235E 15	4.03	24.22
150	1.1814	7617.	0.	202111.	1.04912771E 16	4.03	25.77
155	1.02660	13587.	0.	202111.	1.12078317E 16	4.03	27.27
160	9.6682	2637.	0.	202111.	1.25103864E 16	4.03	28.72
165	7.6311	35467.	0.	202111.	1.35269410E 16	4.03	30.13
170	6.5487	52580.	1.	202111.	1.45394957E 16	4.03	31.43
175	5.6076	74165.	2.	202111.	1.65505015E 16	4.03	32.82
180	4.7964	100226.	6.	202111.	1.63606630E 16	4.03	34.11
185	4.0347	129571.	17.	202111.	1.7571159RE 16	4.03	35.36
190	3.4967	161856.	43.	202111.	1.85377142E 16	4.03	36.58
195	2.9824	195682.	116.	225600.	1.9769720E 16	4.26	37.77
200	2.5407	229716.	270.	25593.	2.05865750F 16	4.53	38.93
205	2.1033	262619.	587.	284660.	2.24109744E 16	4.70	40.6
210	1.8030	293160.	1203.	31212.	2.39750677E 16	5.02	41.16
215	1.5718	3.9301.	2324.	33843.	2.56667510E 16	5.22	42.24
220	1.3369	343256.	4257.	36073.	2.77712637E 16	5.39	43.29
225	1.1405	361511.	7423.	38609.	2.93129565E 16	5.51	44.32
230	9713	374821.	12360.	39693.	3.13574296E 16	5.65	45.32
235	9223	393180.	19724.	41117.	3.34433136E 16	5.75	46.31
240	7045	386785.	30207.	42487.	3.55337489E 16	5.84	47.27
245	6000	395988.	44745.	43673.	3.77174148E 16	5.93	48.21
250	5110	381252.	63962.	45023.	3.99650288E 16	6.02	49.14
255	4351	373103.	88597.	466651.	4.22992843E 16	6.12	50.04
260	3708	352097.	119191.	48493.	4.47242492E 16	6.25	50.93
265	3156	348789.	156066.	508010.	4.72643012E 16	6.39	51.80
270	2687	333709.	196283.	535679.	4.99426979E 16	6.57	52.60
275	2288	327345.	248614.	56843.	5.27839475E 16	6.76	53.50
280	1949	300136.	303535.	6052C.	5.58120382E 16	6.91	54.32
285	1660	282465.	363246.	64731.	5.90489905E 16	7.22	55.13
290	1413	254658.	426710.	692781.	6.25127671E 16	7.73	55.93
295	1203	246986.	492711.	764000.	6.62172973E 16	7.72	56.71
300	1025	229666.	559915.	790506.	7.017317292E 16	7.98	57.48
305	873	212671.	626942.	84086.	7.437317692E 16	8.22	58.23
310	743	195731.	69428.	88902.	7.8822702E 16	8.45	58.92
315	633	181338.	15508H.	937059.	8.35055630E 16	8.64	59.71
320	539	16755.	913763.	981071.	8.84138645E 16	8.83	60.43
325	459	153019.	867458.	102036.	9.35185266E 16	9.05	61.14
330	391	140147.	915365.	1055903.	9.8790502E 16	9.22	61.84
335	333	128136.	956877.	108547.	1.04224733E 17	9.34	62.52
340	283	116974.	991588.	110845.	1.09768977E 17	9.45	63.20
345	241	106635.	101929.	1126159.	1.15999790E 17	9.52	63.87
350	206	97687.	1039925.	113711H.	1.2108587AE 17	9.57	64.53
355	175	84295.	1053635.	114205.	1.26766401E 17	9.59	65.18
360	149	40217.	108666.	116205.	1.32568493E 17	9.59	65.82
365	127	72a12.	1061384.	113422.	1.38174533E 17	9.55	66.45
370	104	66739.	1057366.	112209.	1.43791C8CE 17	9.50	67.07
375	92	59945.	1046379.	110631e.	1.49322557E 17	9.43	67.68

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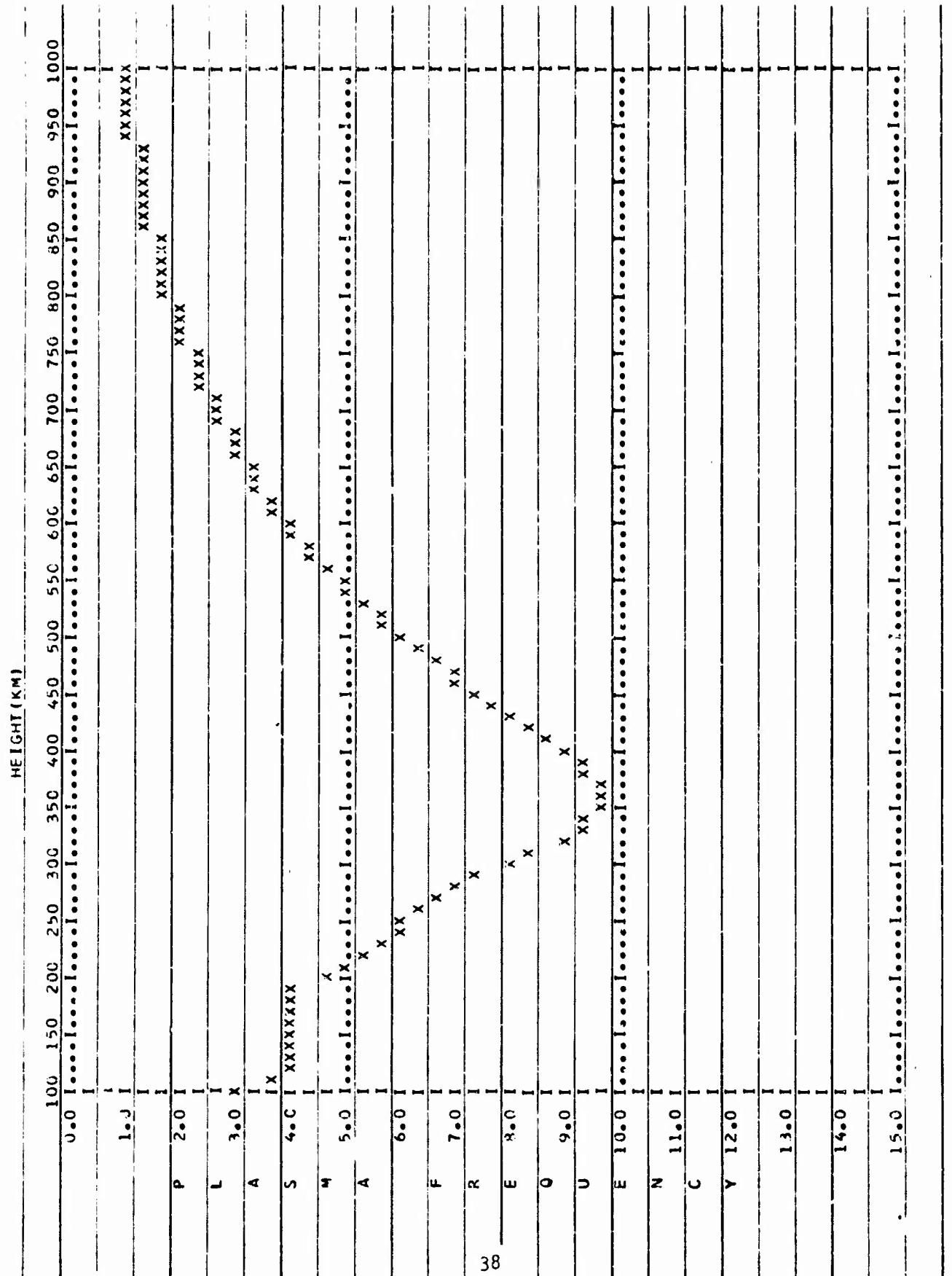
340	78.	54109.	1032163.	1086440.	1.5754858E 17	9.35	68.29
345	67.	45056.	101406.	1.603578.	1.6526334E 17	9.25	68.89
350	57.	44317.	903735.	1038159.	1.6526334E 17	9.14	69.48
355	44.	40124.	97018.	1010891.	1.7031779E 17	9.02	70.06
400	41.	36264.	942163.	942163.	1.7222861E 17	8.89	70.64
405	35.	32761.	91599.	957395.	1.7959058E 17	8.71	71.20
410	30.	29581.	893236.	921943.	1.8660030E 17	8.41	71.77
415	25.	26711.	864375.	891112.	1.8955862E 17	8.67	72.32
420	22.	24108.	836032.	860162.	1.9356672E 17	8.32	72.87
425	18.	21753.	807539.	829311.	1.9503227E 17	8.17	73.41
430	16.	16624.	779102.	798741.	2.0496932E 17	8.02	73.94
435	13.	17697.	768602.	780398.	2.0339938E 17	7.86	74.47
440	11.	15900.	723042.	739013.	2.0035002E 17	7.71	75.00
445	10.	14390.	69574.	71073.	2.1285369E 17	7.56	75.51
450	9.	12912.	66877.	681857.	2.1994650E 17	7.41	76.02
455	7.	11592.	642723.	654621.	2.1926575E 17	7.26	76.53
460	6.	10537.	617266.	627809.	2.205797E 17	7.11	77.03
465	5.	92955.	592548.	602048.	2.2415034E 17	6.96	77.52
470	4.	9555.	568596.	571156.	2.2830191E 17	6.81	78.01
475	4.	7708.	535431.	533142.	2.3106752E 17	6.67	78.50
480	3.	6964.	523060.	530007.	2.3317558E 17	6.53	78.98
485	3.	6755.	501488.	507746.	2.3625628E 17	6.39	79.43
490	2.	5634.	430711.	486347.	2.3668802E 17	6.26	79.92
495	2.	5075.	460721.	465797.	2.4101705E 17	6.12	80.38
500	2.	4516.	441505.	446077.	2.4247390E 17	5.99	80.84
505	1.	4116.	423050.	427167.	2.4318322E 17	5.86	81.30
510	1.	3701.	405337.	409045.	2.4428450E 17	5.74	81.75
515	1.	3338.	388347.	391686.	2.4386888E 17	5.61	82.20
520	1.	3006.	372060.	375067.	2.5126221E 17	5.49	82.64
525	1.	2707.	356453.	359161.	2.5058013E 17	5.34	83.08
530	1.	2337.	341505.	363943.	2.5477730E 17	5.26	83.51
535	1.	2194.	327192.	329387.	2.5424662E 17	5.15	83.94
540	0.	1976.	313491.	315467.	2.5001998E 17	5.04	84.36
545	0.	1779.	30379.	302159.	2.3957791E 17	4.97	84.79
550	0.	1602.	289437.	289437.	2.6095971E 17	4.87	85.20
555	0.	162.	275833.	272776.	2.6346351E 17	4.77	85.62
560	0.	1298.	264355.	265653.	2.6367461E 17	4.62	86.03
565	0.	1169.	253376.	253545.	2.6397734E 17	4.53	86.44
570	0.	1052.	242877.	243922.	2.6616985E 17	4.43	86.84
575	0.	948.	232837.	233782.	2.6733590E 17	4.34	87.24
580	0.	853.	223236.	224089.	2.6865634E 17	4.25	87.63
585	0.	768.	214055.	214823.	2.6853048E 17	4.16	88.03
590	0.	691.	205276.	205967.	2.6756023E 17	4.07	88.42
595	0.	622.	196880.	197503.	2.7547809E 17	3.98	88.80
600	0.	560.	188552.	189412.	2.72494870E 17	3.90	89.18
605	0.	504.	181175.	181678.	2.7403226E 17	3.82	89.56
610	0.	454.	173830.	174295.	2.7427468E 17	3.74	89.94
615	0.	403.	166807.	167215.	2.7511075E 17	3.67	90.31
620	0.	364.	160088.	160456.	2.7591303E 17	3.59	90.66
625	0.	331.	153661.	153922.	2.7668299E 17	3.52	91.05
630	0.	298.	147511.	147809.	2.77422204E 17	3.45	91.42
635	0.	269.	141627.	141896.	2.7813172E 17	3.38	91.78
640	0.	242.	135997.	136238.	2.7881270E 17	3.31	92.16
645	0.	218.	130608.	130826.	2.7946683E 17	3.24	92.49
650	0.	196.	125450.	125646.	2.8095065E 17	3.18	92.87
655	0.	176.	120513.	120685.	2.80698509E 17	3.12	93.20
660	0.	159.	11795.	115944.	2.8127826E 17	3.05	93.54
665	0.	143.	1119.	111402.	2.8193523E 17	2.99	93.89
670	0.	129.	106424.	107053.	2.8237049E 17	2.93	94.23
675	0.	116.	102712.	102886.	2.82864938E 17	2.88	94.57

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680	0	104.	98795.	98900.	2.83379433E 17	2.82	94.91
685	0	64.	94985.	95079.	2.83379433E 17	2.77	95.25
690	0	87.	91334.	91419.	2.84311917E 17	2.71	95.58
695	0	76.	87835.	87911.	2.86751475E 17	2.66	95.91
700	0	68.	84432.	84550.	2.85174227E 17	2.61	96.24
705	0	62.	81267.	81329.	2.85580871E 17	2.56	96.56
710	0	55.	78186.	78241.	2.85972077E 17	2.51	96.89
715	0	50.	75230.	75280.	2.86348477E 17	2.46	97.21
720	0	45.	72396.	72441.	2.86710683E 17	2.41	97.53
725	0	40.	69678.	69719.	2.87059274E 17	2.37	97.84
730	0	36.	67070.	67107.	2.81394807E 17	2.32	98.16
735	0	33.	64569.	64601.	2.87717813E 17	2.28	98.47
740	0	30.	62168.	62197.	2.88028798E 17	2.24	98.78
745	0	27.	59466.	59891.	2.80326251E 17	2.20	99.09
750	0	24.	57653.	57677.	2.80611301E 17	2.15	99.39
755	0	22.	55530.	55551.	2.88894388E 17	2.11	99.70
760	0	19.	53491.	53511.	2.89161938E 17	2.07	100.00
765	0	17.	51534.	51552.	2.89419696E 17	2.04	100.30
770	0	16.	49655.	49670.	2.89668044E 17	2.00	100.60
775	0	14.	47849.	47863.	2.85907360E 17	1.96	100.89
780	0	13.	46115.	46127.	2.90137994E 17	1.93	101.19
785	0	11.	44448.	44500.	2.90360290E 17	1.89	101.48
790	0	10.	42847.	42857.	2.90574574E 17	1.86	101.77
795	0	9.	41308.	41317.	2.90781158E 17	1.82	102.06
800	0	8.	39829.	39837.	2.90980542E 17	1.79	102.34
805	0	7.	38607.	38614.	2.91172406E 17	1.76	102.63
810	0	6.	37039.	37046.	2.91357636E 17	1.73	102.91
815	0	6.	35725.	35731.	2.91536289E 17	1.70	103.19
820	0	5.	34460.	34466.	2.91708615E 17	1.67	103.47
825	0	5.	33244.	33249.	2.91878622E 17	1.64	103.75
830	0	4.	32071.	32079.	2.9235258E 17	1.61	104.03
835	0	4.	30949.	30953.	2.9390021E 17	1.58	104.30
840	0	4.	29867.	29870.	2.93339373E 17	1.35	104.58
845	0	3.	28825.	28828.	2.92483512E 17	1.22	104.85
850	0	3.	27822.	27825.	2.9622632E 17	1.50	105.12
855	0	2.	26857.	26859.	2.97756927E 17	1.57	105.39
860	0	2.	25927.	25930.	2.92886576E 17	1.44	105.65
865	0	2.	25033.	25035.	2.93011749E 17	1.42	105.92
870	0	2.	24173.	24173.	2.93132612E 17	1.39	106.18
875	0	2.	23342.	23343.	2.9249330E 17	1.37	106.44
880	0	2.	22543.	22544.	2.93362051E 17	1.35	106.70
885	0	1.	21773.	21775.	2.93470919E 17	1.32	106.96
890	0	1.	21032.	21033.	2.93576083E 17	1.30	107.22
895	0	1.	20318.	20319.	2.93777676E 17	1.28	107.48
900	0	1.	19629.	19630.	2.93775824E 17	1.26	107.73
905	0	1.	18956.	18967.	2.93870555E 17	1.25	107.99
910	0	1.	18327.	18328.	2.93962294E 17	1.21	108.24
915	0	1.	17711.	17711.	2.94050848E 17	1.19	108.49
920	0	1.	17117.	17117.	2.94136432E 17	1.17	108.74
925	0	1.	16544.	16545.	2.94219154E 17	1.15	108.99
930	0	1.	15992.	15993.	2.94269114E 17	1.13	109.23
935	0	0.	15460.	15480.	2.94376415E 17	1.12	109.48
940	0	0.	14946.	14947.	2.94451147E 17	1.10	109.72
945	0	0.	14451.	14452.	2.9452300E 17	1.08	109.96
950	0	0.	13974.	13974.	2.94593266E 17	1.06	110.21
955	0	0.	13513.	13513.	2.94660930E 17	1.04	110.45
960	0	0.	13068.	13068.	2.94726169E 17	1.03	110.69
965	0	0.	12639.	12640.	2.94789368E 17	1.01	110.92
970	0	0.	12225.	12226.	2.94850492E 17	0.99	111.16
975	0	0.	11826.	11826.	2.94909620E 17	0.98	111.39



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100	1.20	4.03
100	1.20	4.03
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100	1.20	4.53
100	1.20	6.02
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100	1.20	9.22
100	350	6.57
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100	400	8.89
100	500	5.95
100	600	3.95
100	750	2.15
100	900	1.20
100	1000	0.90

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13. ABSTRACT

This paper describes a project undertaken by 4th Weather Wing to produce a realistic electron density profile based upon parameters which can be forecast with reasonable accuracy. The ionospheric electron density profile model presented in this paper consists of the sum of three Chapman layers (E, F1, F2). Electron densities in the topside ionosphere are controlled by complex motions rather than a production-loss balance and cannot be successfully described strictly by a Chapman layer. After some experimentation a best fit was obtained by simply using the Chapman equation for the topside ionosphere, but computing the electron densities by using a variable scale height throughout the region. The program described in this report has been used routinely for eight months to predict profiles for radar refraction. This report should be considered interim as improvements in accuracy are sure to be required as the model is evaluated for different purposes.